

|  | <b>Course name:</b> MATH 535 Combinatorics  |     |                     |          |       | <b>Department:</b> Mathematics |          | Semester      |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
|--|---|-----|---------------------|----------|-------|--------------------------------|----------|---------------|-------|----------|---|---|---|--|---|------------|---|----------------------------|---|------------------------------|---|---|---|--|---|-------------------------------------|---|-----------------------------|----|-------------------|----|-----------------------------------|----|-----------------------|----|---------------------------------|----|-------------------|
|  |   |     |                     |          |       |                                |          | <b>1</b>      |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
|  | Methods of Education  |     |                     |          |       |                                |          | Credit (ECTS) |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| Lecture  | Recitation/ (Etud)  | Lab | Project/Field Study | Homework | Other | Total                          | <b>8</b> |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 42   | 0   | 0   | 90                  | 60       | 48    | 240                            |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| Language   | English   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| Compulsory/Elective  | Departmental Elective   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| Prerequisites  | None  |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| Course Description   | Generating functions, recurrence relations, extremal problems for graphs and set systems, probabilistic methods in combinatorics, algebraic methods in combinatorics.   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| Course Contents  | <table border="1"> <thead> <tr> <th>Weeks</th> <th>Subjects</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>Binomial Coefficients, Generating Function Models</td> </tr> <tr> <td>2</td> <td>Calculating Coefficients of Generating Functions</td> </tr> <tr> <td>3</td> <td>Partitions</td> </tr> <tr> <td>4</td> <td>Recurrence Relation Models</td> </tr> <tr> <td>5</td> <td>Divide-and-Conquer Relations</td> </tr> <tr> <td>6</td> <td>Solution of Linear Recurrence Relations</td> </tr> <tr> <td>7</td> <td>Solution of Inhomogeneous Recurrence Relations</td> </tr> <tr> <td>8</td> <td>Solutions with Generating Functions</td> </tr> <tr> <td>9</td> <td>Review, <b>Midterm Exam</b></td> </tr> <tr> <td>10</td> <td>Extremal Problems</td> </tr> <tr> <td>11</td> <td>Basic Probability, Expected Value</td> </tr> <tr> <td>12</td> <td>Probabilistic Methods</td> </tr> <tr> <td>13</td> <td>Basic Linear Algebra, Dimension</td> </tr> <tr> <td>14</td> <td>Algebraic Methods</td> </tr> </tbody> </table> |     |                     |          |       |                                |          |               | Weeks | Subjects | 1 | Binomial Coefficients, Generating Function Models | 2 | Calculating Coefficients of Generating Functions | 3 | Partitions | 4 | Recurrence Relation Models | 5 | Divide-and-Conquer Relations | 6 | Solution of Linear Recurrence Relations | 7 | Solution of Inhomogeneous Recurrence Relations | 8 | Solutions with Generating Functions | 9 | Review, <b>Midterm Exam</b> | 10 | Extremal Problems | 11 | Basic Probability, Expected Value | 12 | Probabilistic Methods | 13 | Basic Linear Algebra, Dimension | 14 | Algebraic Methods |
| Weeks  | Subjects  |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 1  | Binomial Coefficients, Generating Function Models   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 2  | Calculating Coefficients of Generating Functions  |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 3  | Partitions  |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 4  | Recurrence Relation Models  |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 5  | Divide-and-Conquer Relations  |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 6  | Solution of Linear Recurrence Relations   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 7  | Solution of Inhomogeneous Recurrence Relations  |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 8  | Solutions with Generating Functions   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 9  | Review, <b>Midterm Exam</b>   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 10   | Extremal Problems   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 11   | Basic Probability, Expected Value   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 12   | Probabilistic Methods   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 13   | Basic Linear Algebra, Dimension   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| 14   | Algebraic Methods   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| Course Objectives  | This course will focus on some basic concepts in combinatorics and provide methods to solve combinatorial problems.   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| Learning Outcomes and Competences  | <p>By a successful completion of this course, students should be able to:</p> <ol style="list-style-type: none"> <li>1. Understand basic concepts in combinatorics</li> <li>2. Solve linear recurrence relations</li> <li>3. Apply basic probabilistic and algebraic methods on combinatorial problems</li> </ol>   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |
| Textbook and /or References  | <p><b>References:</b></p> <ul style="list-style-type: none"> <li>• Joy Morris, Combinatorics, 2017</li> <li>• Alan tucker, Applied Combinatorics, Wiley, 2012</li> <li>• Alon, Noga and Joel H. Spencer. The Probabilistic Method. Wiley, 2016</li> </ul>   |     |                     |          |       |                                |          |               |       |          |   |   |   |  |   |            |   |                            |   |                              |   |   |   |  |   |                                     |   |                             |    |                   |    |                                   |    |                       |    |                                 |    |                   |

|  |                             |                 |                 |                        |
|--|-----------------------------|-----------------|-----------------|------------------------|
| Assessment Methods and Criteria          | <b>In-Term Studies</b>      |                 | <b>Quantity</b> | <b>Percentage%</b>     |
|  | Mid-terms                   |                 | 1               | 25                     |
|  | Quizes                      |                 | 0               | 0                      |
|  | Assignments                 |                 | 3               | 25                     |
|  | Attendance                  |                 | 0               | 0                      |
|  | Practice                    |                 | 0               | 0                      |
|  | Project                     |                 | 1               | 20                     |
|  | Final Examination           |                 | 1               | 30                     |
| <b>Total</b>                             |                             | <b>6</b>        | <b>100</b>      |                        |
| ECTS Allocated Based on Student Workload | <b>Activities</b>           | <b>Quantity</b> | <b>Duration</b> | <b>Total Work Load</b> |
|  | Course Duration             | 14              | 3               | 42                     |
|  | Hours for off-the-c.r.study | 14              | 5               | 70                     |
|  | Assignments                 | 3               | 20              | 60                     |
|  | Mid-terms                   | 1               | 20              | 20                     |
|  | Project                     | 1               | 20              | 20                     |
|  | Final Examination           | 1               | 28              | 28                     |
| <b>Total</b>                             | <b>34</b>                   | <b>96</b>       | <b>240</b>      |                        |
| Instructors                              |                             |                 |                 |                        |